

# Airdrop games

And other blockchain launch models

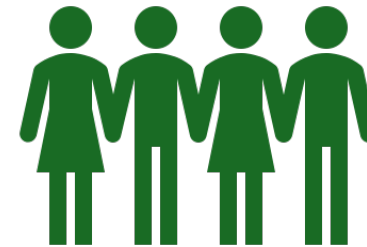
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Edinburgh 6.12.2024

# Launching a new blockchain



Several open questions



Success depends on enough people being convinced of value of the project and/or to contribute

Public good?

# Public Goods

- Definition: Non rivalrous/non excludable (Samuelson 1954)
- Problem: free riding!
- Why?
- A. Smith (1776): Street lamps
  - One person enjoys, does not detract from other person's enjoyment
  - Can't charge every person for amount they use

# Public goods games

- Classic type of game in experimental economics
- N players
- Endowment  $w$
- Can contribute  $x$ , cost  $c(x)$
- Contributions are summed, multiplied and distributed to all
- Output per capita  $o(X)$ ,  $X = \sum x_i$
- Individual utility  $U = w - c(x_i) + o(X)$
- $O'$  is marginal per capita return
- Linear case  $w - x + mX$
- Individual rationality: corner solution, invest all if  $m > 1$ , else nothing
- Collective rationality: invest all if  $m > 1/N$

**SUBMITTED**

# “Airdrop games”

## logit dynamics in a contribution game

- A specific case of a public goods game
  - That we think corresponds well to the blockchain case with miners/SPOs
- Success depends on these players contributing
- Classic Nash: best response
  - Either contribute or not
  - Just do what gives higher payoff, even if difference is  $\epsilon$
- Logit: better response
  - Allows for experimentation
  - Logit dynamics select Nash equilibria (“good” equilibria)
  - Even if noise vanishing!

# Why logit?

- Allows for experimentation
  - $P_i = \exp(\beta U_i) / \sum \exp(\beta U)$
  - where  $i=1, \dots, I$  all possible actions
- Plenty of support in experimental economics
- Nash + logit fits behavior well
  - In simple normal form games, mixed strategy equilibria, traveler's dilemma, auctions...
- Even better, logit equilibrium (QRE)

# Logit dynamics

- Players choose sequentially
- In each period, one chosen and informed of number of contributors
- Decide on action
  - (Not a complete, contingent strategy)
  - But better respond, not best
  - According to logit rule

# Parameters

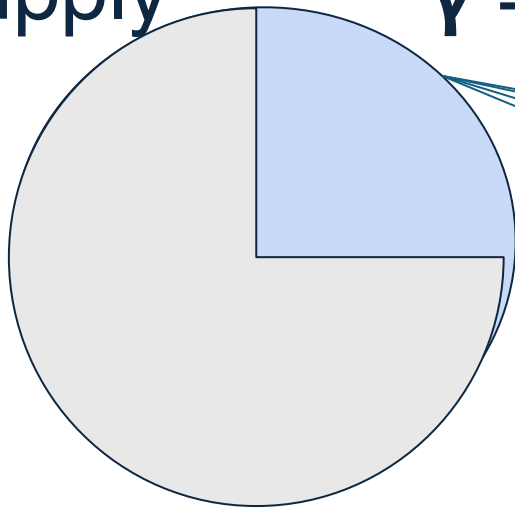
1.  $\gamma$  = rewards (anyway)
2.  $\alpha$  = cost (if contributing)
3.  $\beta$  = rationality level

Limited  $\rightarrow$  Interesting Considerations

Token\_supply

$$\gamma = \rho \times \text{Token\_supply}$$

$$\rho \leq 1$$





Example

## Threshold “technology”

$V(\mathbf{a}) = \text{“high” or “low”}$  if at least 50% contribute

## Quadratic “technology”

$V(\mathbf{a}) = I^2$  for  $I = \text{“number of contributors”}$

# Bad and good Nash equilibria

None contributes

50% contribute

Why do good equilibria appear?

# “Noisy” best response model

- Even in cases where free riding is best response,  $m < 1$  (threshold makes no difference)
- Some people might experiment
- If enough do, then the next player becomes pivotal
- For pivotal player contribution is clearly a best response

# Results

# Tradeoffs

1. Higher costs (and/or smaller noise) → More time
2. Rewards don't accelerate convergence...
3. ...but help to maintain good equilibrium

# Non vanishing noise

**Theorem 6.** *For any threshold technology (32) with airdrop rewards (2) and any inverse noise parameter  $\beta > 0$ , the probability of selecting the high value outcome (33) is monotone increasing in the rewards  $\rho$  and, in particular, it has the following form:*

$$p_{high}(\rho) = \frac{1}{1 + C \cdot \exp(-\rho B)} \quad B = \frac{\beta}{n} \cdot (V_{high} - V_{low}), \quad (35)$$

where  $C = C(\alpha\beta, n, \tau) = \frac{1 - p_{high}(0)}{p_{high}(0)}$  does not depend on rewards  $\rho$  nor on the values  $V_{low}$  and  $V_{high}$ .<sup>4</sup>

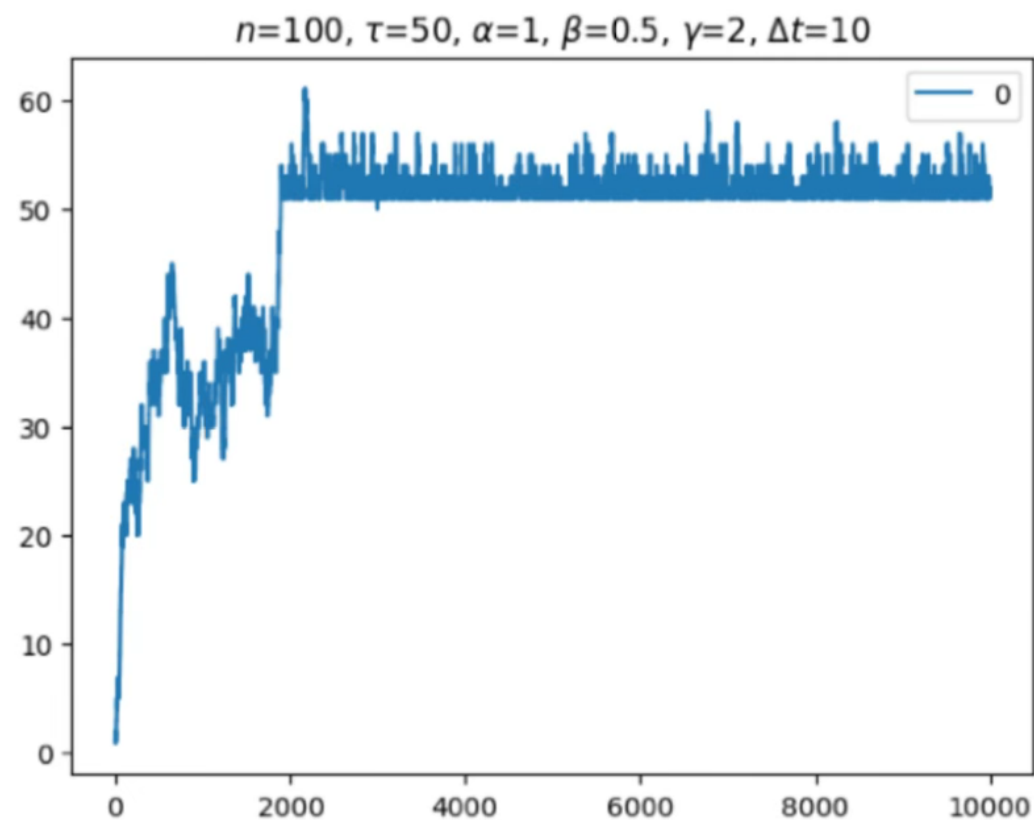
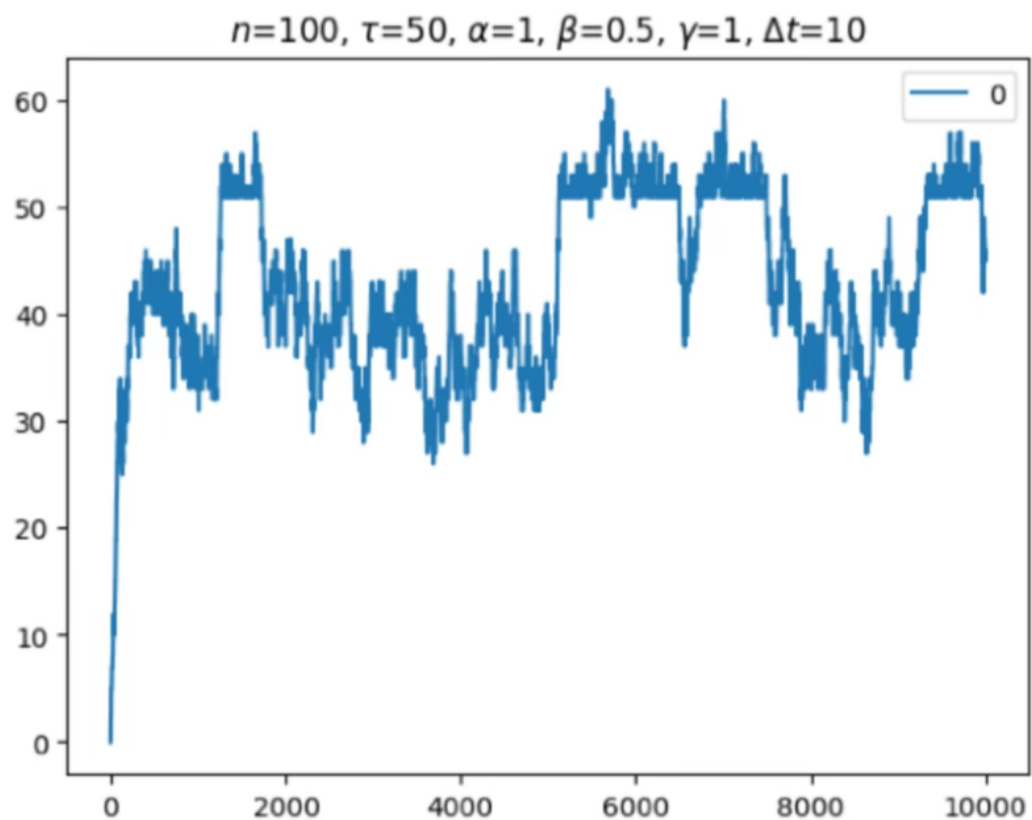


# Average contribution level

$$\ell^* = n \cdot p_{\alpha\beta}, \quad p_{\alpha\beta} := \frac{1}{1 + \exp(\alpha\beta)}$$

- Only depends on  $\alpha\beta$

# Rewards stabilize dynamics



# Tradeoffs

1. Higher costs (and/or smaller noise) → More time
2. Rewards don't accelerate convergence...
3. ...but help to maintain good equilibrium

## “Technology” matters

1. Quadratic  $\neq$  Threshold...

## Partnerchain framework application

1. Reduced cost (Cardano SPOs), do not pay in ADA

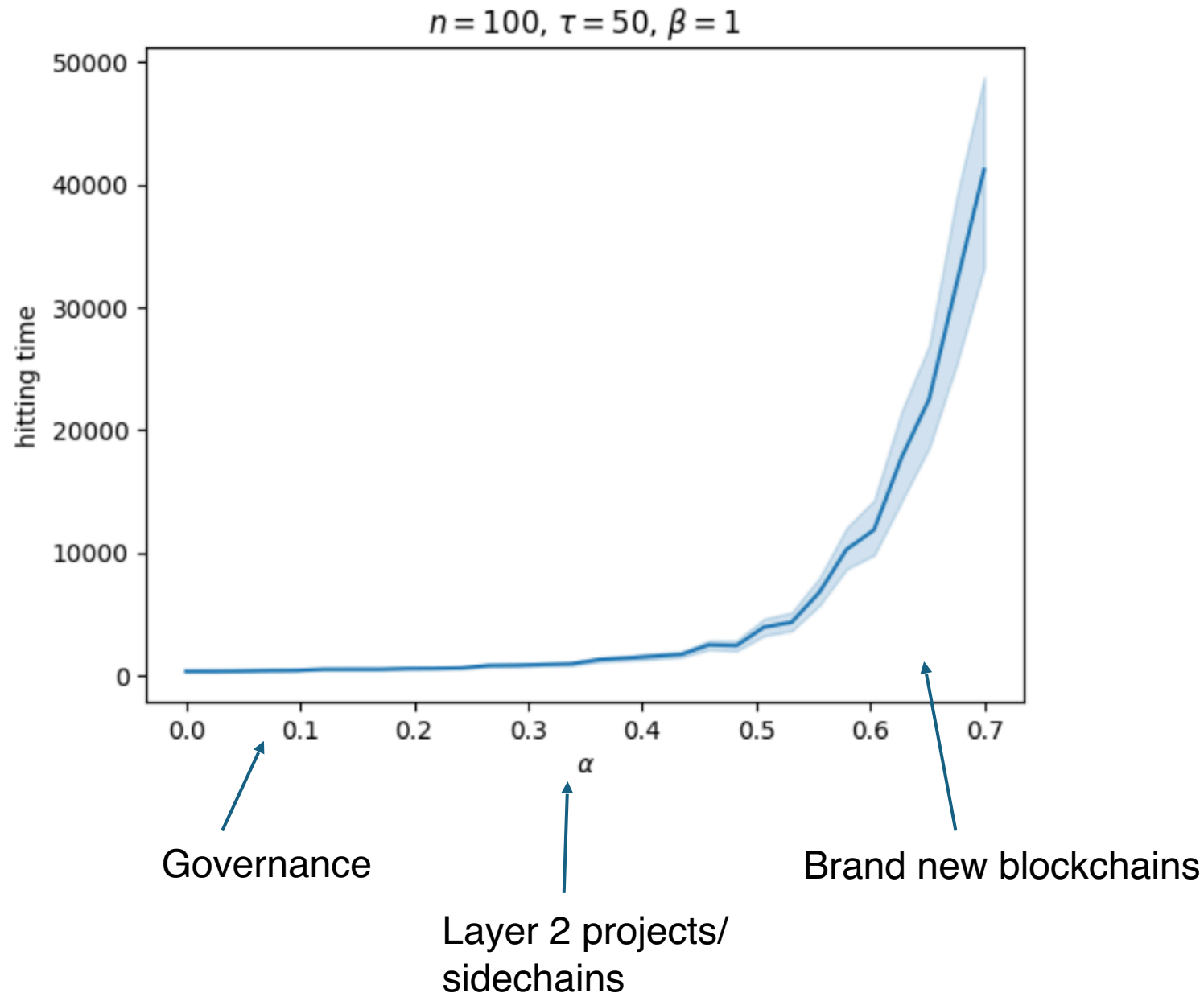
# General Framework

1. Technology value  $V(a)$
2. Good vs bad equilibria, role of rewards (and other parameters)

## Designer Strategy

1. Low airdrop  $\rightarrow$  No contribution  $\rightarrow$  Fail
2. High  $\rightarrow$  Contribution, but not convenient for designer
3. Medium  $\rightarrow$  Contribution + good (profit) for designer ?

Application:  
3 cases  
depending on  
contribution  
cost



# Newest results (next paper?)

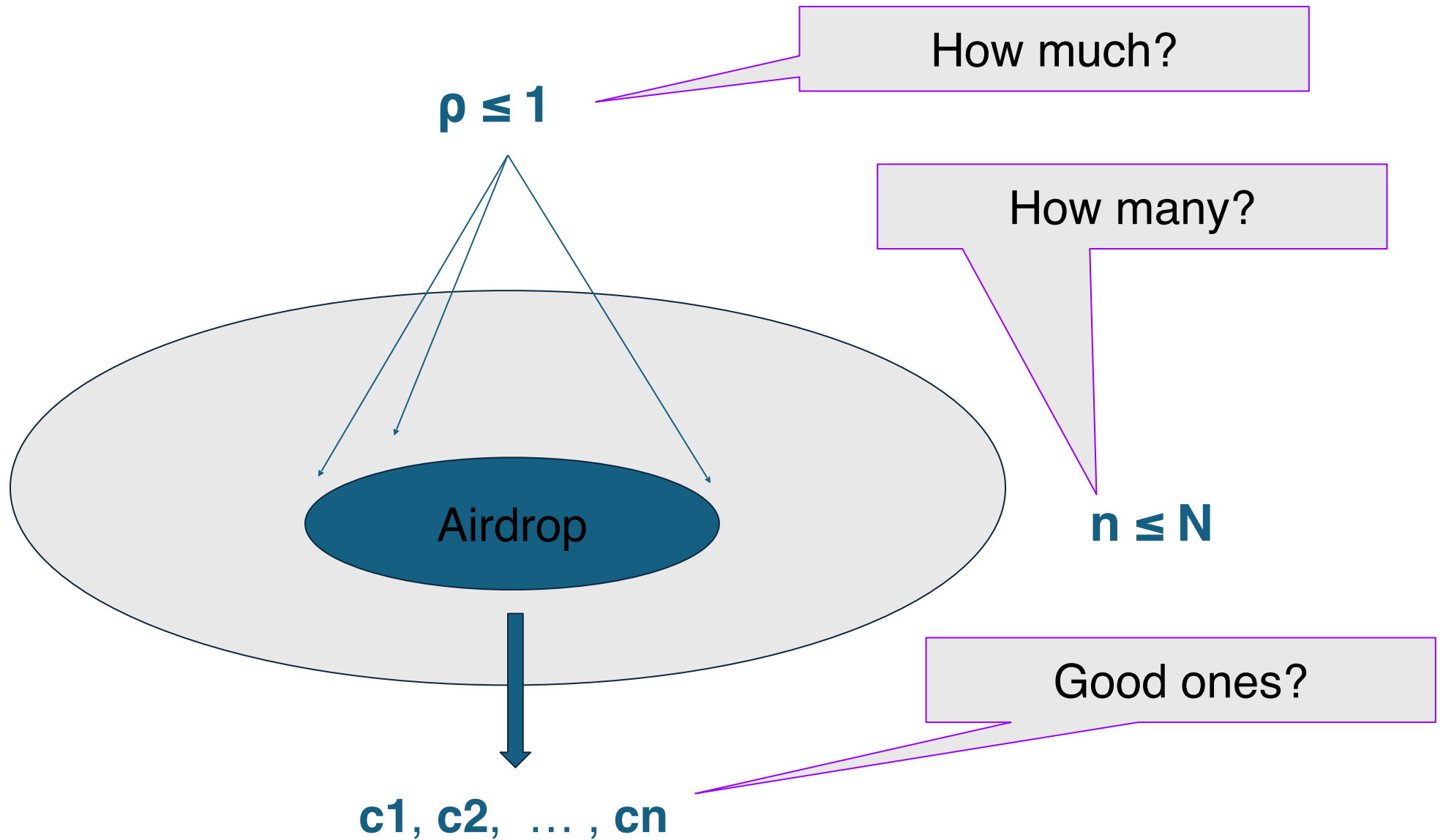
- Suppose designer observes total contribution result in every period
- Gives every token holder rewards proportional to that sum
  - even if they didn't contribute
- This can help achieve the good equilibrium
- And can be beneficial for designer
  - (Making sure that rewards calibrated to not cause much inflation)

# Conclusions

- Logit dynamics allow for high contribution equilibria (known)
- The exact technology matters
- In some cases partnering with an existing blockchain helps, because it lower costs of experimentation

# Appendix





Dissipation of airdrop (rewards):  $\rho/n$  each vs costs  $c_i$

1. Designer chooses  $\rho$
2. Players reach some (pure Nash) **equilibrium  $\mathbf{a}$**
3. Value of system is  $V(\mathbf{a})$  and price of token  
$$t(\mathbf{a}) = V(\mathbf{a}) / (\text{Token supply})$$

## Further results:

1. **Characterization of equilibria** (higher  $\rho \rightarrow$  higher contributions  $\mathbf{a} \rightarrow$  higher system value and token price), heterogeneous costs too.
2. **Highest possible system value** for  $\rho = 1$  (“bad” technologies/design result in “low” contribution  $\rightarrow$  “low” value).
3. **Tradeoffs** (system value, social cost, social welfare, designer’s profit)

# Appendix

## Model 2: Signalling

- The information that is provided by the issuers can be thought of as a (potentially costly) signal
- How do receivers of the signal process it?
- Are they convinced to buy/contribute?

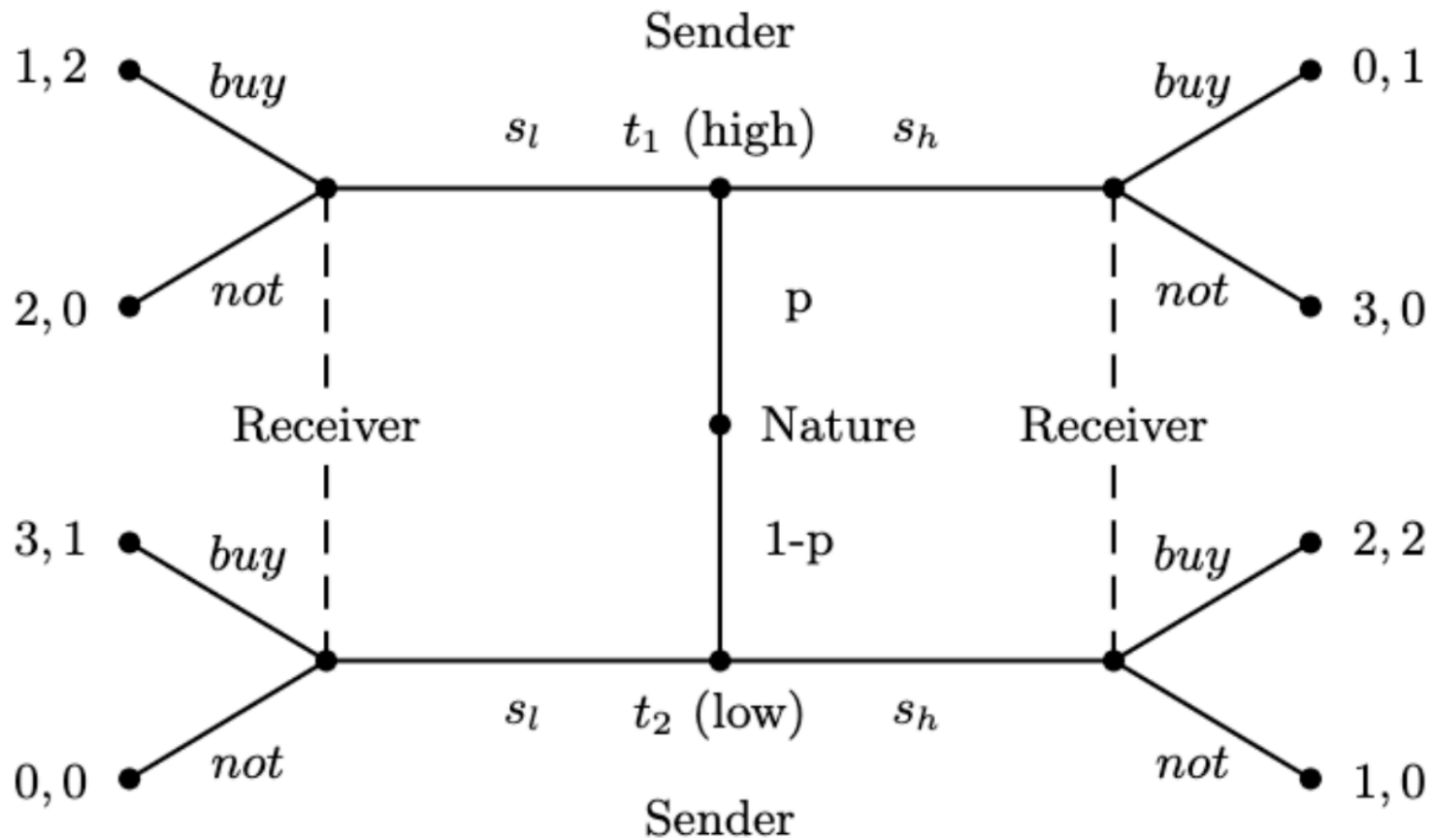
# Spence (1973) job signalling

- Questions:
  - How much effort (time, cost) should signal sender spend?
  - How reliable is the signal?
  - Is there a good signalling equilibrium?
- Spence's application: education and jobs
  - How do job candidates signal skills?
  - What is the role of education?

# Education signalling

- Two groups of people, I and II
  - Proportion  $p$  and  $1-p$
  - Cost of education level  $y$  is:  $y$  and  $y/2$
  - Marginal productivity: 1 and 2
- Employer believes there is educ. threshold  $y^*$  for which marginal productivity is:
  - 1 if  $y < y^*$
  - 2 if  $y > y^*$
  - Offers wages equal to MP
- If signalling effective
  - group I chooses  $y=0$  if  $1 > 2 - \frac{y}{2}$
  - group II chooses  $y=y^*$  if  $2 - \frac{y}{2} > 1$
- $1 < y^* < 2$ , so beliefs are confirmed

# Separating equilibria and effective signalling



Separation:

Each type sends a different signal  
 Bayesian receiver perfectly  
 knows who is who

High type happy not with separation

Low type also not!

# From education to IPOs

- Leland & Pyle (1977) analyze signals in IPOs
- Good companies should send clear signals
  - the owner should keep control of a significant percentage of the company
- Signal needs to be reliable
  - Bad companies should find imitation hard
- Other strategies possible
  - Underpricing

# What about ICOs

- Need to estimate payoffs and prior beliefs
  - Payoffs of good vs bad tokens
  - Belief that a given token, before seeing any signal, is of "high quality"
- Also to consider what signals can be sent
  - How many?
  - Dimensions?
  - Types?
- Test the signals?



# Getting data to check/test hypotheses

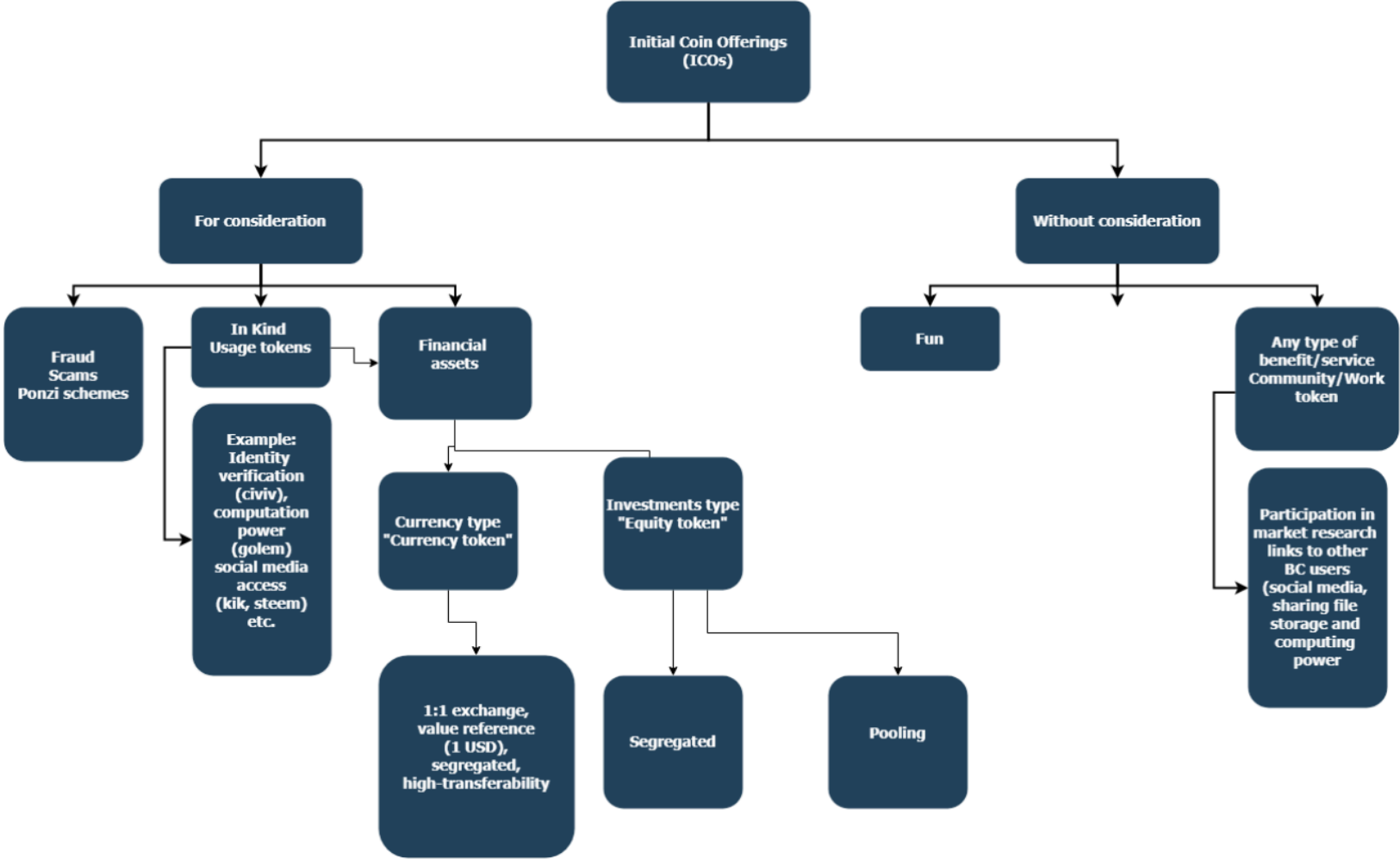
- Field data
  - Coinmarketcap
  - Coingecko
  - Other aggregators...
  
- Survey/experiment data
  - Who to target?

# I. Field data

## Building an ICO database

- It seems around 25,000 cryptocurrencies exist
- Large heterogeneity in
  - Quality
  - Purpose
  - Success!

# ICO taxonomy



# Current database

- 7200 ICOs
  - from 2016 to 2020
- 11 sources
  - Etherscan.io, coindesk, coingecko, cryptocompare, ICObench, ICODrops, ICOrating, ICOmarks, icodata, Foundic, TokenData
  - Merging info and choosing most trustworthy
- ICO characteristics
  - % for sale
  - Hardcap
  - Whitelist
  - Kyc
  - Team member size
  - Presale
- Socia media
  - Reddit
  - Twitter
  - Medium

# Summary descriptives

Variable	Mean	Std. dev.	Min	Median	Max	Obs.
Panel A: ICO variables						
ICO characteristics						
<i>hardcap</i>	294.73	9,371.63	0.00	20.00	523,000.00	3,698
<i>% for sale</i>	0.56	0.24	0.00	0.57	1.00	3,938
<i>presale</i>	0.52	0.50	0.00	1.00	1.00	5,450
<i>presale raised</i>	0.04	0.19	0.00	0.00	1.00	5,450
<i>kyc</i>	0.50	0.50	0.00	1.00	1.00	5,450
<i>whitelist</i>	0.40	0.49	0.00	0.00	1.00	5,450
<i># team members</i>	10.62	8.02	1.00	9.00	74.00	3,476
ICO outcomes						
<i>raised dummy</i>	0.45	0.50	0.00	0.00	1.00	5,450
<i>amount raised, conditional on raising (US\$ million)</i>	13.11	89.68	0.00	3.80	4,197.96	2,473
<i>raised-to-hardcap, conditional on raising</i>	0.44	0.39	0.00	0.29	1.00	1,950
<i>listing</i>	0.41	0.49	0.00	0.00	1.00	2,473

# How many ICOs are successful?

Variable	Mean	Std. dev.	Min	Median	Max	Obs.
ICO end-to-open returns						
<i>ICO return, conditional on listing (%)</i>	384.39	936.82	2.96	46.25	3,870.72	1,007
<i>ICO return, unconditional (%)</i>	99.75	646.98	-100.00	-100.00	3,870.72	2,442
ICO first-day returns						
<i>ICO first day return (%)</i>	9.71	22.82	-19.67	1.62	75.86	1,170
Longer-term cumulative post-ICO returns						
<i>30-day return (%)</i>	-2.64	80.38	-78.60	-29.69	233.42	1,159
<i>90-day return (%)</i>	-0.22	127.45	-94.33	-47.70	415.91	1,136
<i>180-day return (%)</i>	-7.74	149.40	-97.65	-70.43	489.57	1,083
<i>365-day return (%)</i>	-38.03	110.38	-99.28	-85.04	337.34	894

# Analysis: what determines ICO success

Variable	(1) <i>raised dummy</i>	(2) <i>log(amount raised + 1)</i>	(3) <i>raised-to-hardcap</i>	(4) <i>listing dummy</i>
<i>% for sale</i>	-0.073* (-1.759)	-1.504** (-2.240)	-0.133*** (-4.806)	-0.214*** (-6.333)
<i>hardcap (log)</i>	0.001 (0.179)	0.362*** (2.877)	-0.033*** (-5.918)	0.010 (0.740)
<i>whitelist</i>	-0.021 (-0.994)	-0.006 (-0.017)	0.058*** (2.921)	0.034 (0.901)
<i>kyc</i>	0.160*** (4.718)	2.580*** (5.354)	0.124*** (6.482)	0.221*** (6.939)
<i>white paper</i>	0.039** (2.024)	0.687** (2.560)	0.051*** (4.208)	0.057** (2.205)
<i>team members size (log)</i>	0.084*** (6.079)	1.347*** (5.905)	0.043*** (3.467)	0.067*** (3.877)
<i>presale</i>	-0.008 (-0.369)	-0.179 (-0.575)	-0.026* (-1.740)	0.033** (2.088)
<i>Commits at ICO start (log)</i>	0.020*** (4.394)	0.298*** (4.542)	0.016*** (4.762)	0.021*** (4.223)
<i>Twitter at ICO start (log)</i>	-0.002 (-0.442)	-0.027 (-0.421)	0.002 (0.489)	-0.010** (-2.190)
<i>Reddit at ICO start (log)</i>	-0.010** (-2.402)	-0.151** (-2.376)	-0.013*** (-4.625)	-0.035*** (-5.342)
<i>BTCTalk at ICO start (log)</i>	0.029*** (10.135)	0.432*** (8.988)	0.006** (2.120)	0.011*** (2.950)
<i>Medium at ICO start (log)</i>	0.009 (1.025)	0.178 (1.472)	0.021*** (3.435)	0.021*** (3.591)
Observations	2,322	2,364	2,364	1,292
R <sup>2</sup>	0.201	0.284	0.310	0.333
Year-month fixed effects	Yes	Yes	Yes	Yes
Industry sector fixed effects	Yes	Yes	Yes	Yes
Geographical region dummy	Yes	Yes	Yes	Yes

# Analysis: focus on % and amount raised

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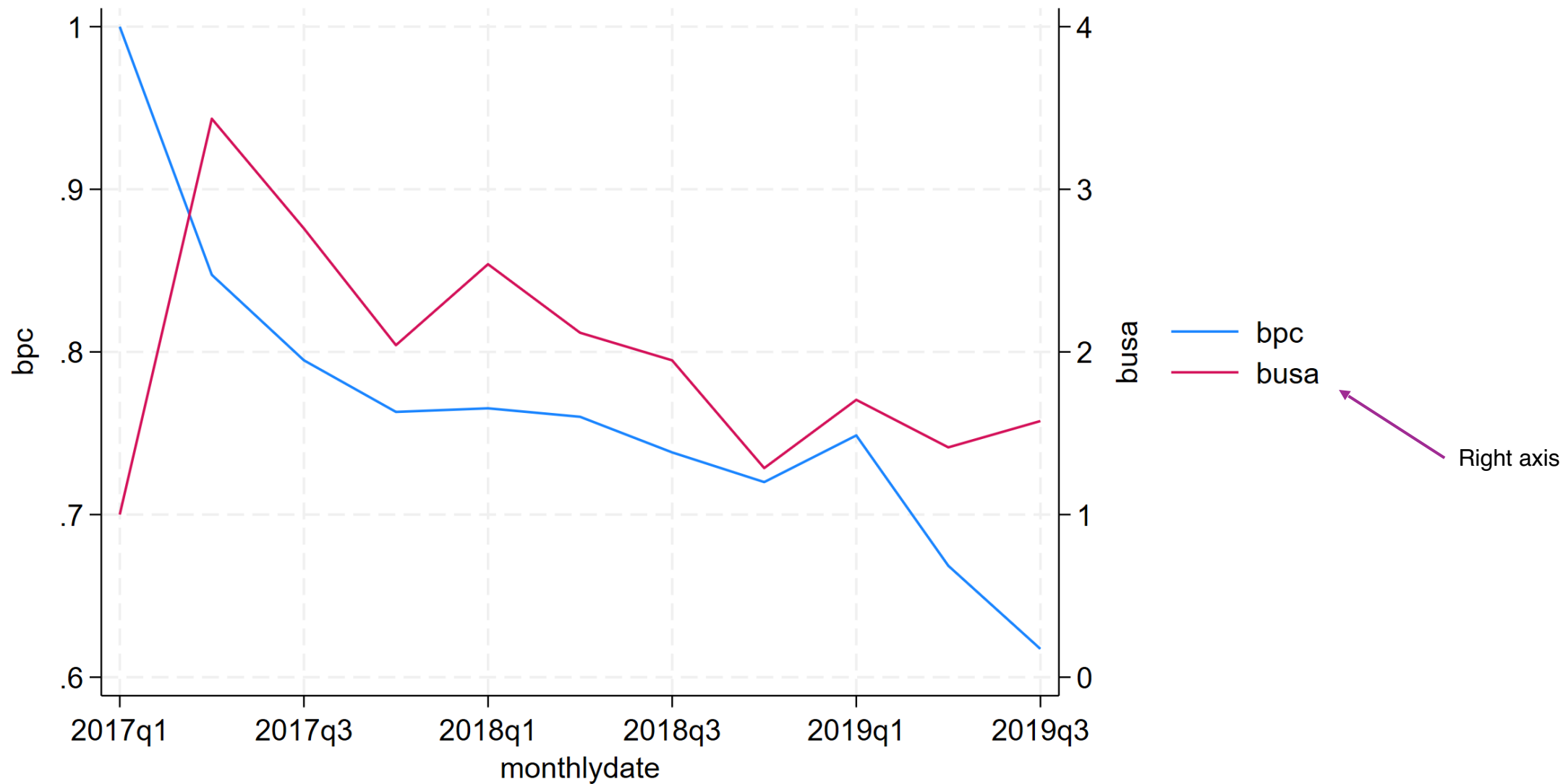
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# Timeseries

- What changes over time?
  - Presale?
  - % sale?
  - Team size
  - Kyc
  - Others?

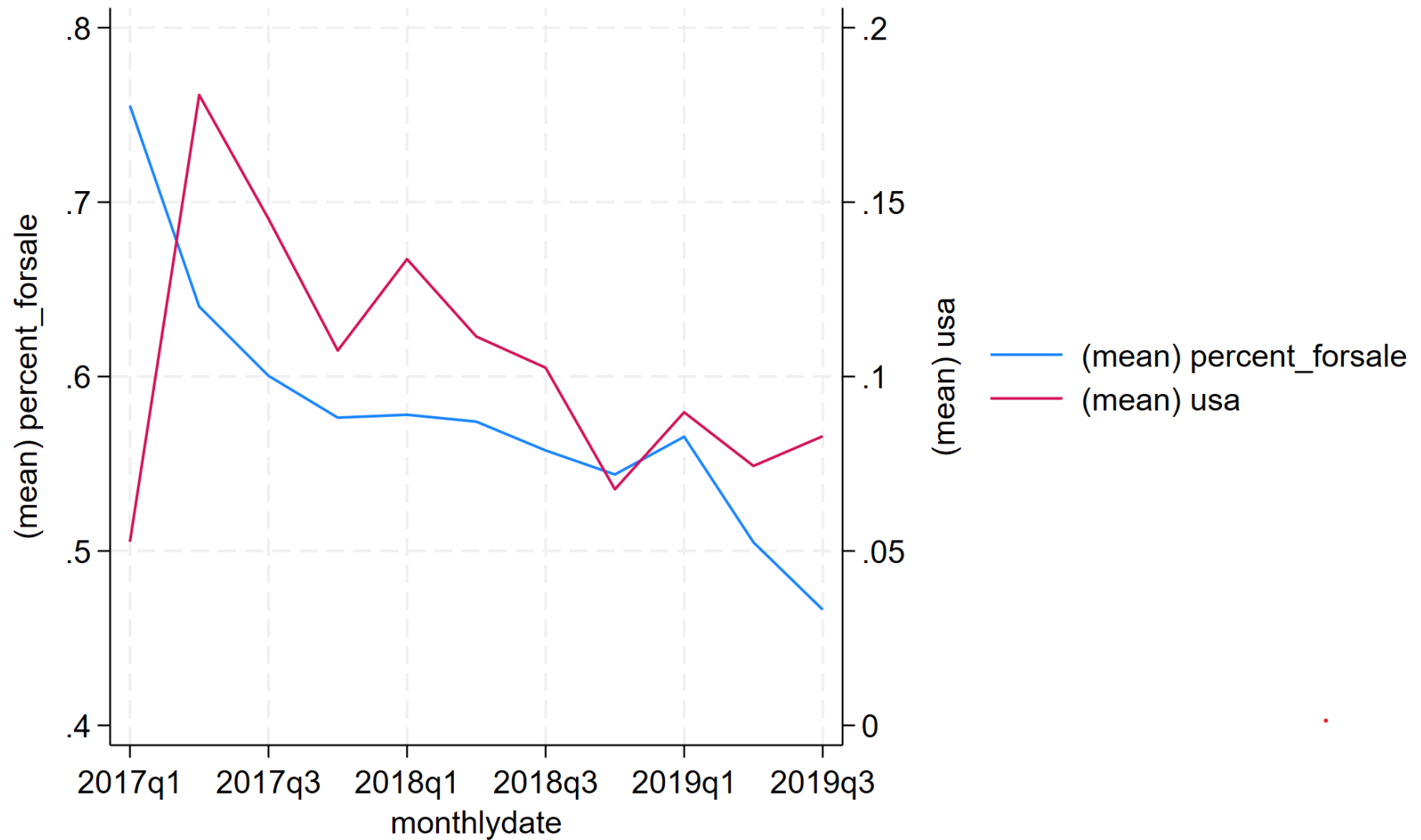
# Timeseries

2017 q1 as baseyear



# Timeseries

absolute



# Expanding the ICO database

- Newer data
  - Harder because variety increased, NFT, defi etc
- Getting data (in the case of the major ICOs?) on exact airdrop strategy, relation with previous blockchains (partnerchain) etc