



THE UNIVERSITY  
*of* EDINBURGH



# Do Blockchain Systems Achieve Decentralization?

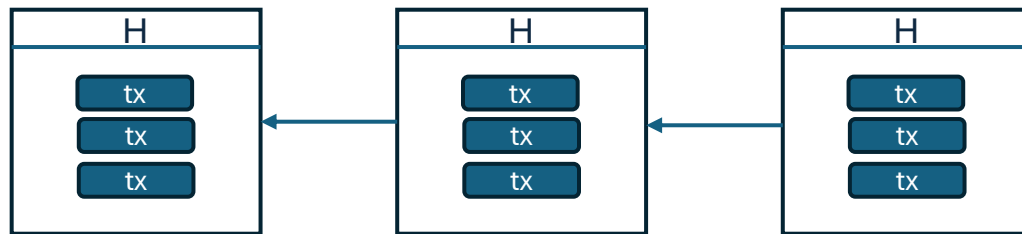
Christina Ovezik

AGT@Blockchains Workshop - WINE 2024

Based on work with Aggelos Kiayias, Dimitris Karakostas, Daniel Woods

# What is a blockchain?

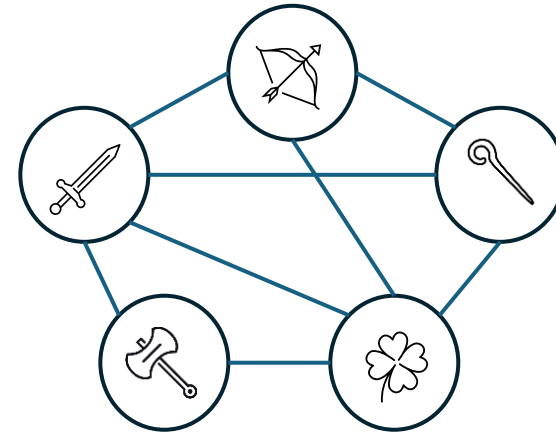
- Digital ledger that satisfies a set of liveness and safety properties, **“without relying on trust”**
- Mechanism design perspective: a protocol with **decentralisation** as an objective



# Centralised vs Decentralised systems



- A **single party** has full control over the system (“rules them all”)
- If it misbehaves or crashes, the system is compromised, e.g.:
  - Censorship
  - Inconsistency
  - Data loss / unavailability



- A number of **independent parties** collectively control the system and guarantee its properties
- If only few nodes are malicious / faulty, the system remains operational
  - No single points of failure

# Example of centralised system failure

**BBC** Sign in Home News Sport Weather iPlayer Sounds

## NEWS

Home | InDepth | Israel-Gaza war | War in Ukraine | Climate | UK | World | Business | Politics | Culture

Technology

### CrowdStrike IT outage affected 8.5 million Windows devices, Microsoft says



EPA

**Joe Tidy**  
Cyber correspondent, BBC News

20 July 2024

# Blockchains are multi-layered systems

- **8 layers of** blockchain systems where **(de)centralisation** can occur
- **Centralisation** in some layer **threatens** desirable system properties, such as **safety, liveness, privacy and price stability**

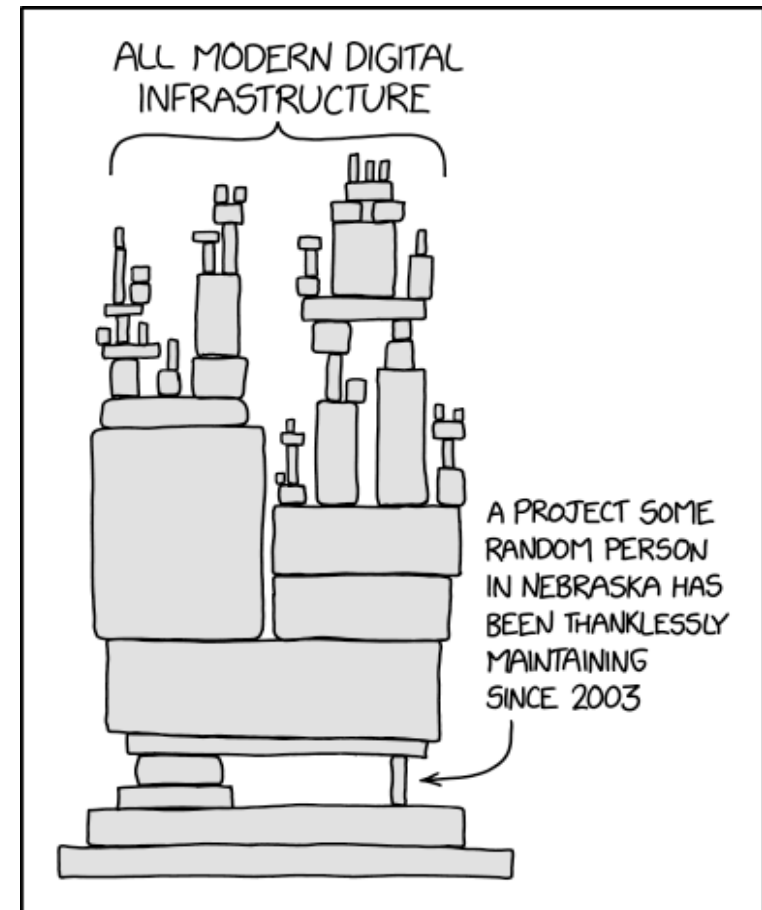
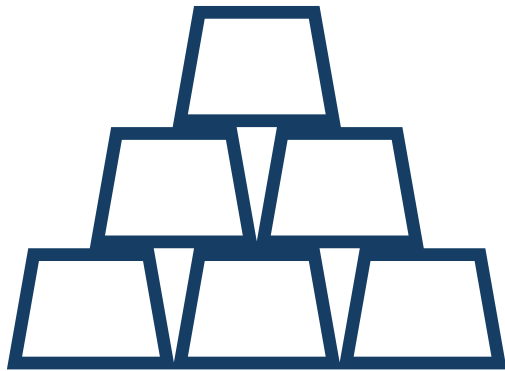


Image credit: <https://xkcd.com/2347/>

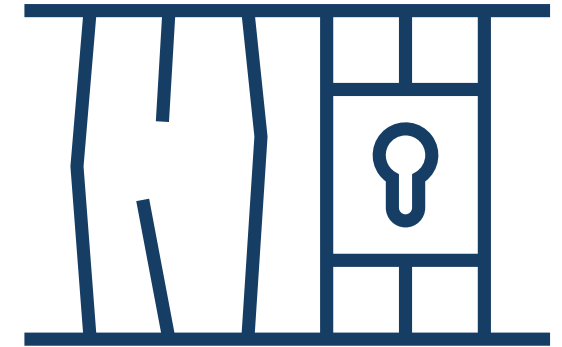
# For each layer



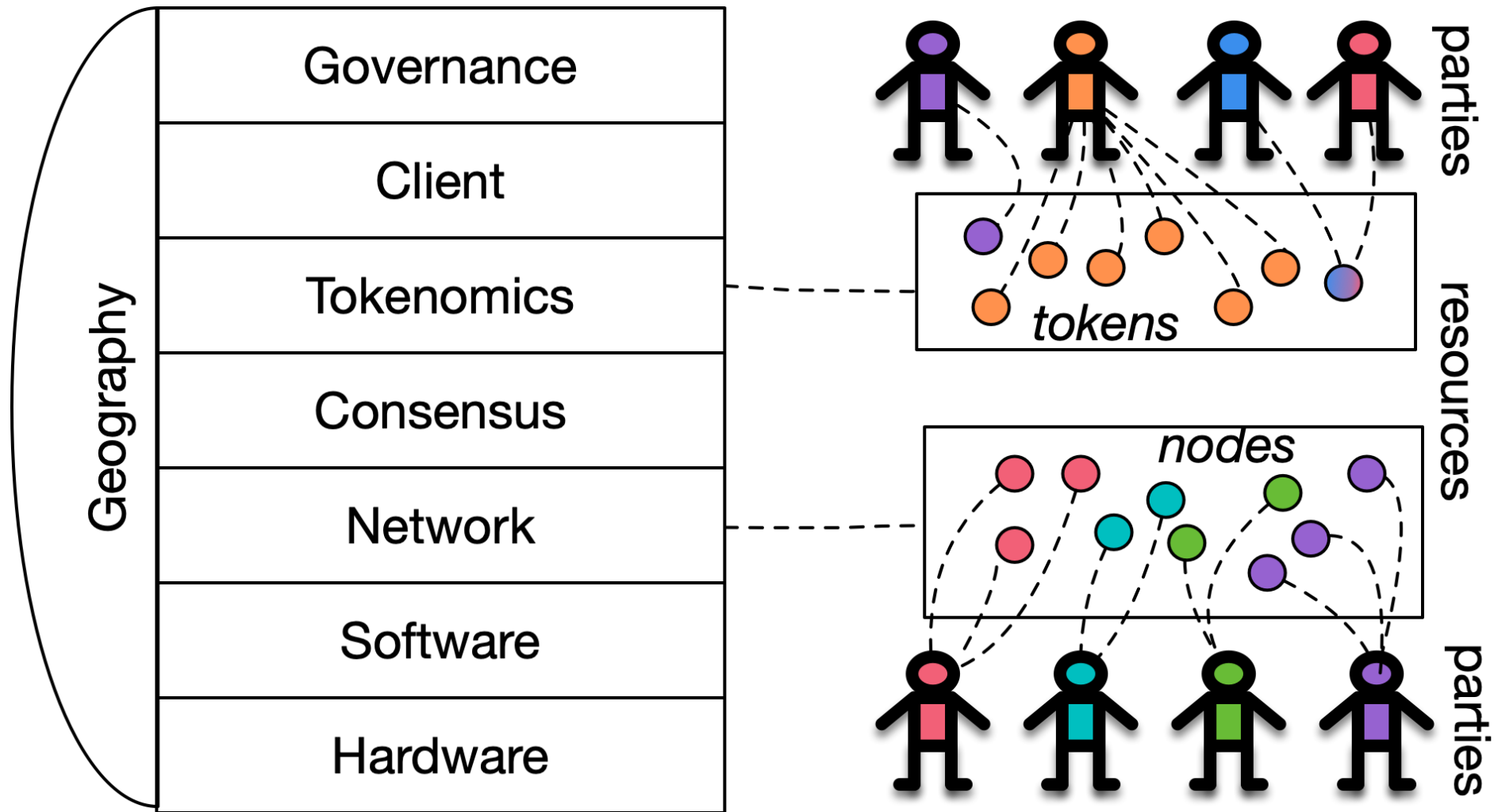
Resource



Relevant  
parties



Properties  
at risk



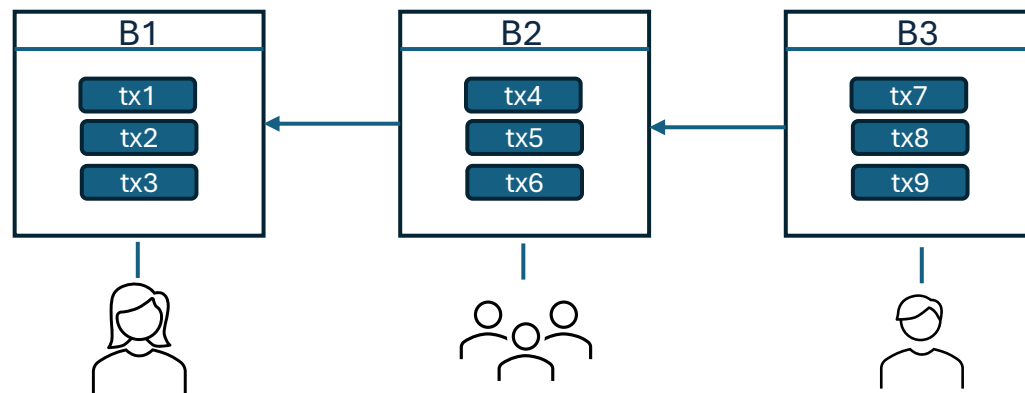
# Case study: consensus layer

Measuring the decentralisation of block production

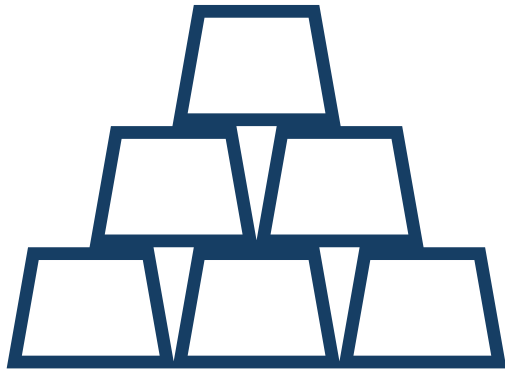


# Consensus layer: extending the blockchain

- Block creators:
  - Decide which transactions get included in a block
    - and in what order
  - Receive rewards for each new block
- The more blocks one creates the more influence they have in the system



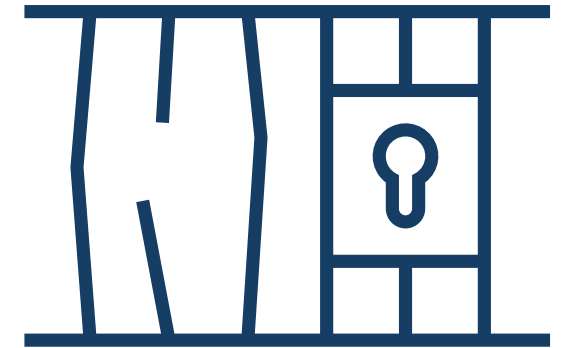
# Consensus – Decentralization Analysis



Resource  
=  
Blocks



Relevant parties  
=  
Block  
producers



Properties  
at risk  
=  
Safety / Liveness

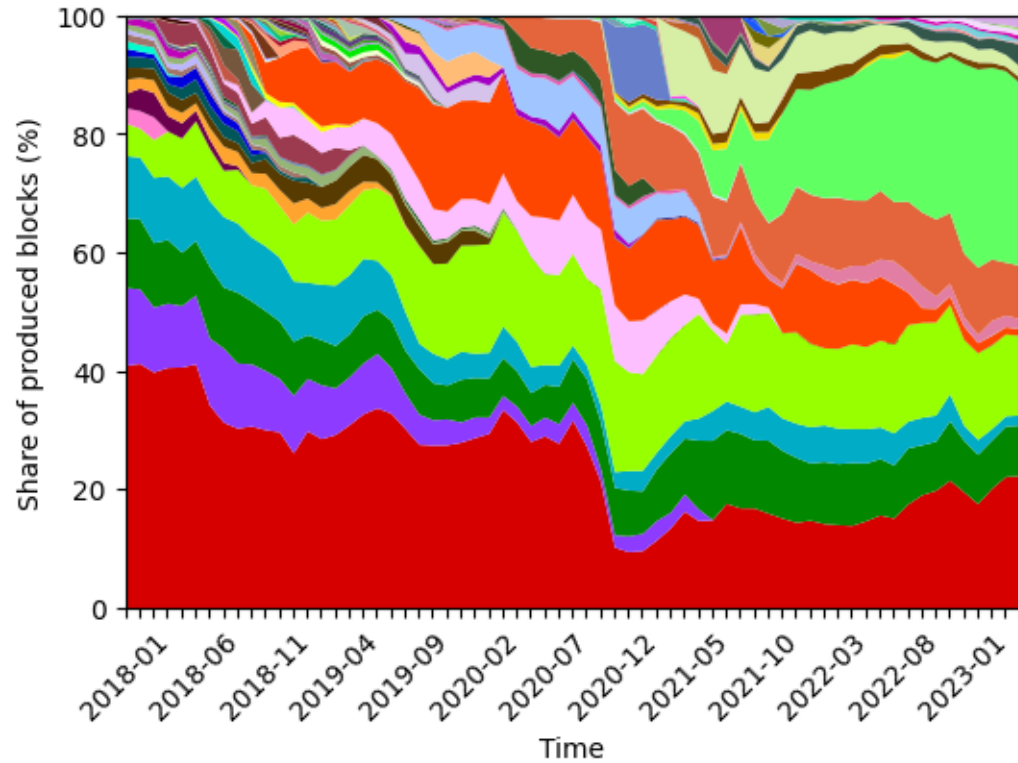
# Mining and the formation of coalitions

- Economies of scale incentivize the formation of coalitions (**mining / stake pools**) with their leaders consolidating disproportionate power
- We treat each such coalition as a single entity

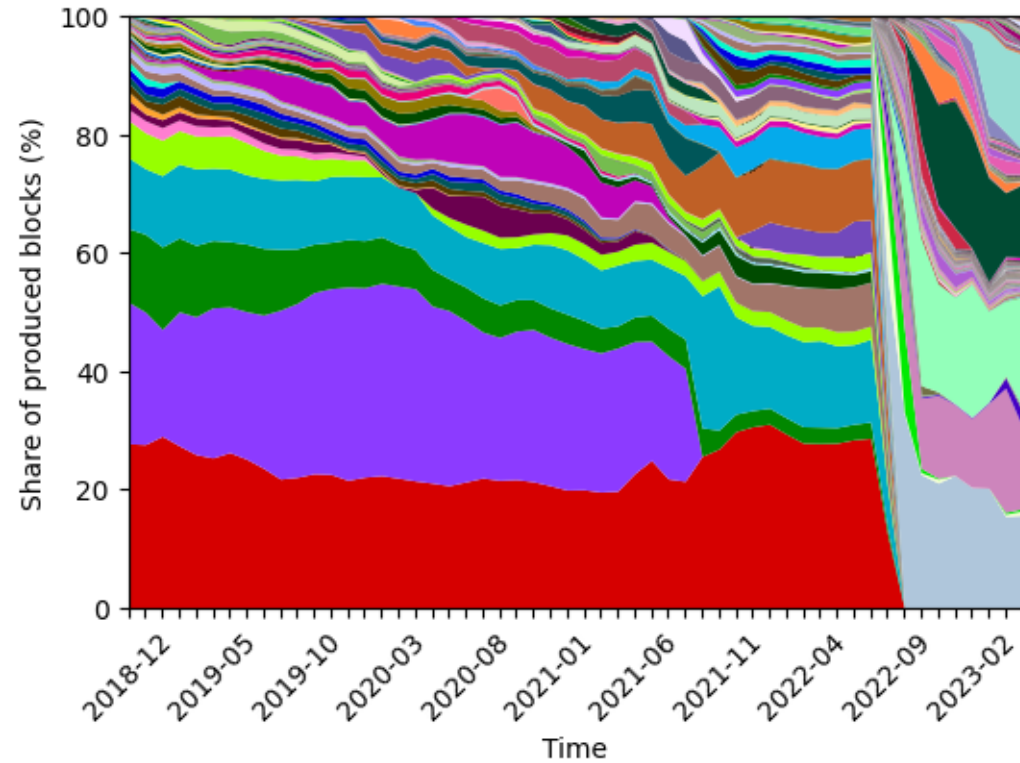


# Block production dynamics

## Bitcoin

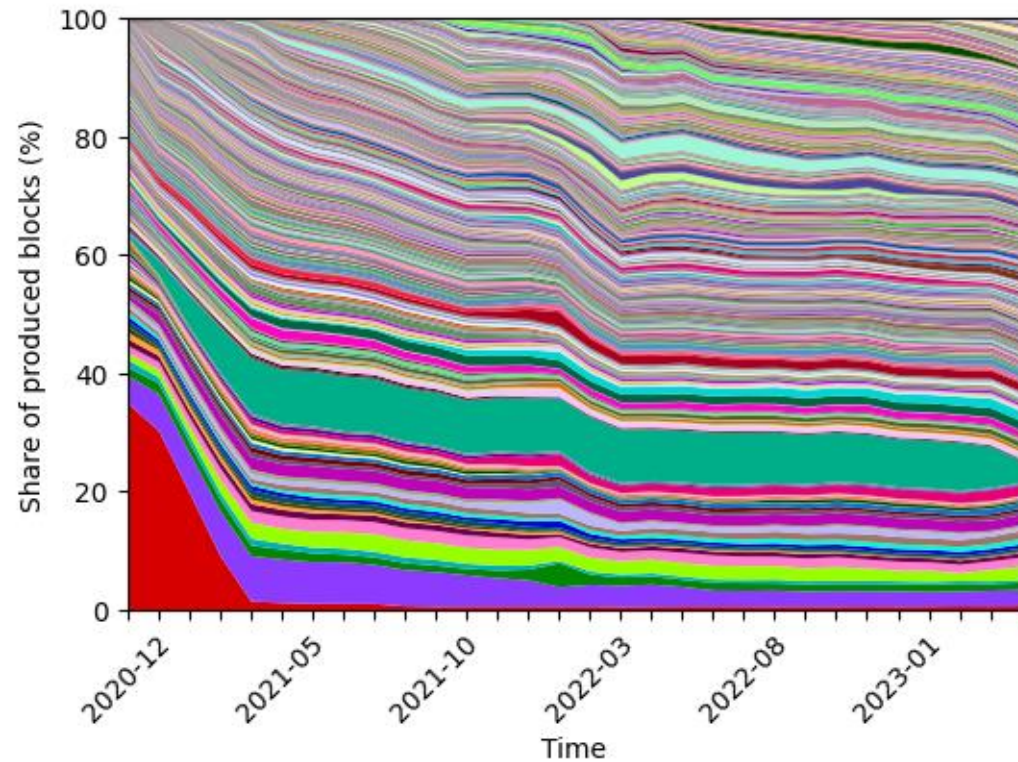


## Ethereum

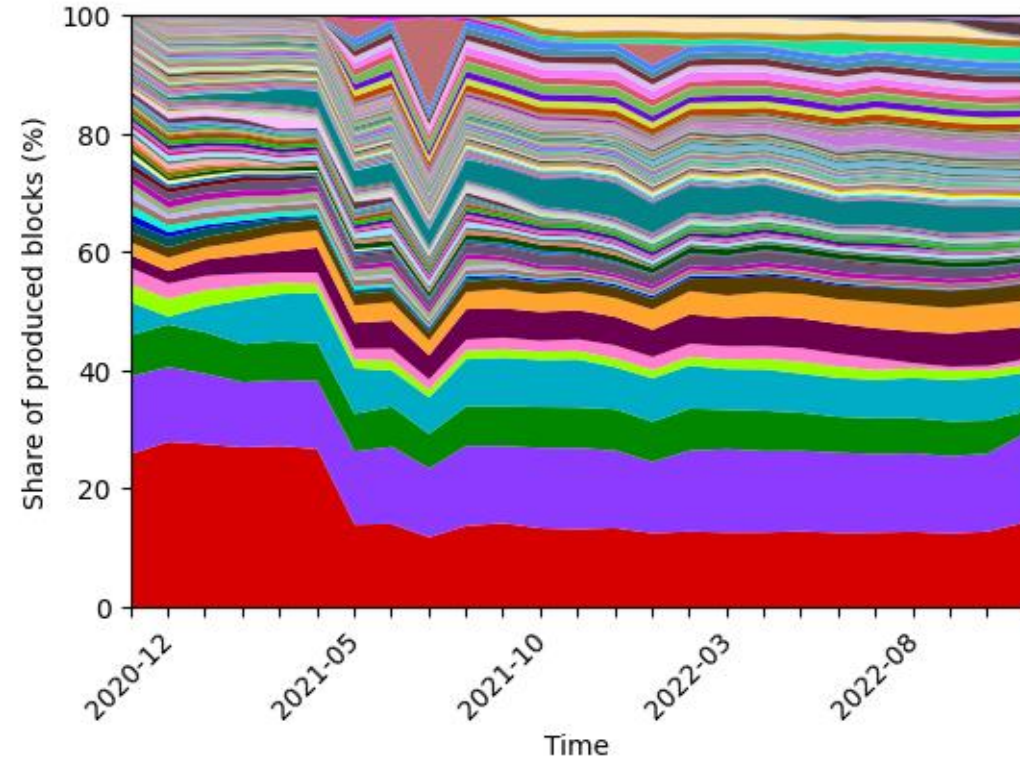


# Block production dynamics

## Cardano



## Tezos

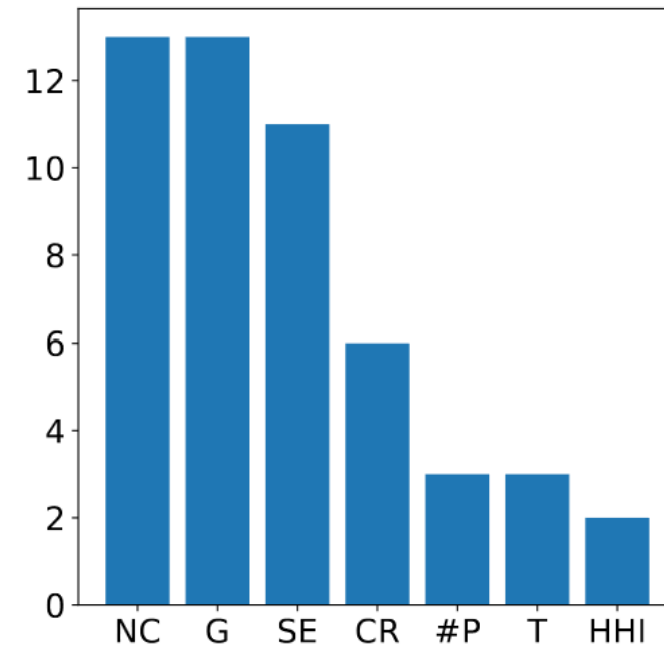




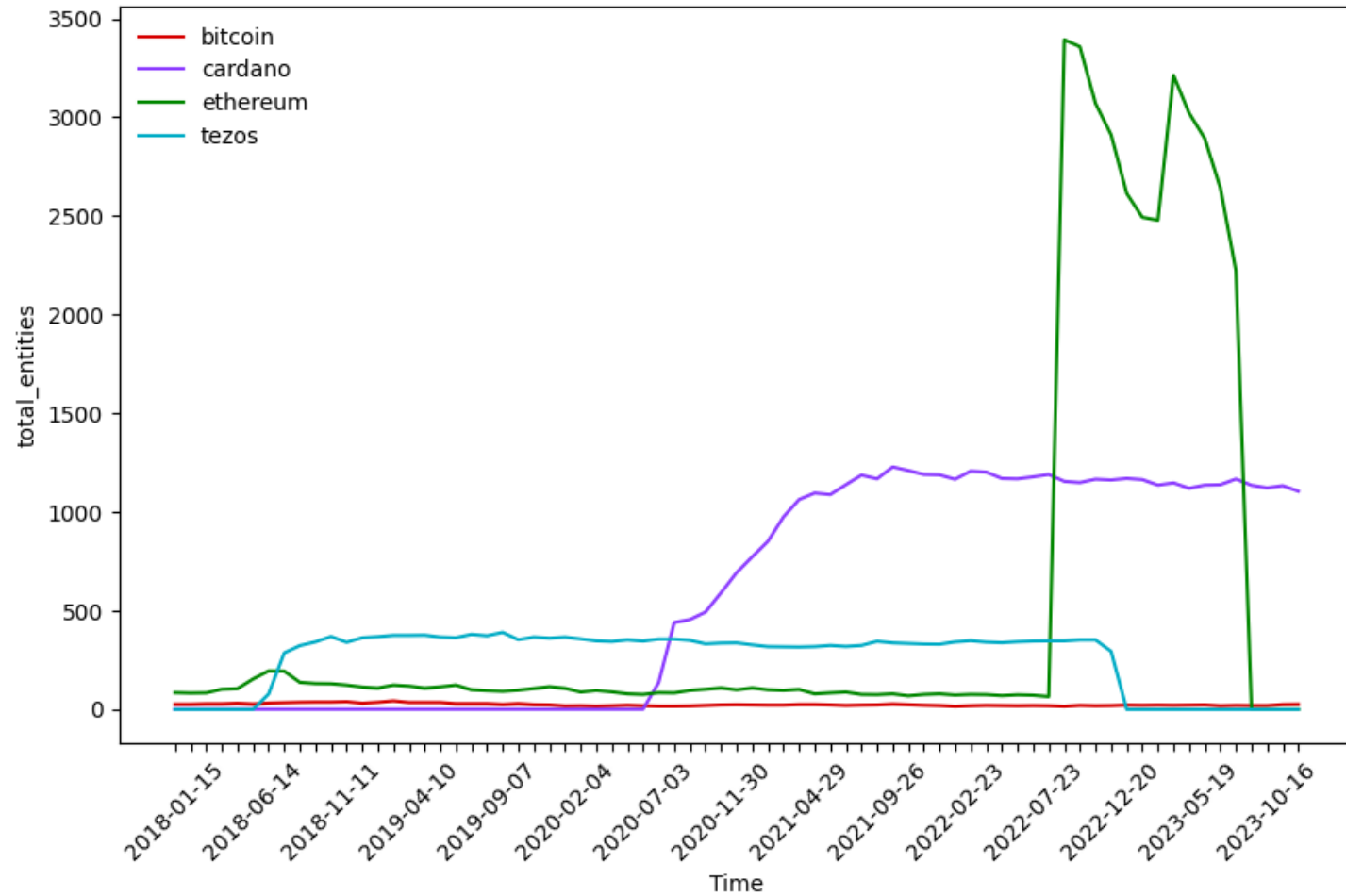
# Decentralization metrics

- Assign a value that represents the decentralization of a distribution
- Metrics used in the blockchain decentralization literature:
  - Nakamoto coefficient (NC)
  - Gini coefficient (G)
  - Shannon entropy (SE)
  - Herfindahl–Hirschman index (HHI)
  - Concentration ratios (CR)
  - Number of parties (P)

Metric usage in the literature



# Number of parties



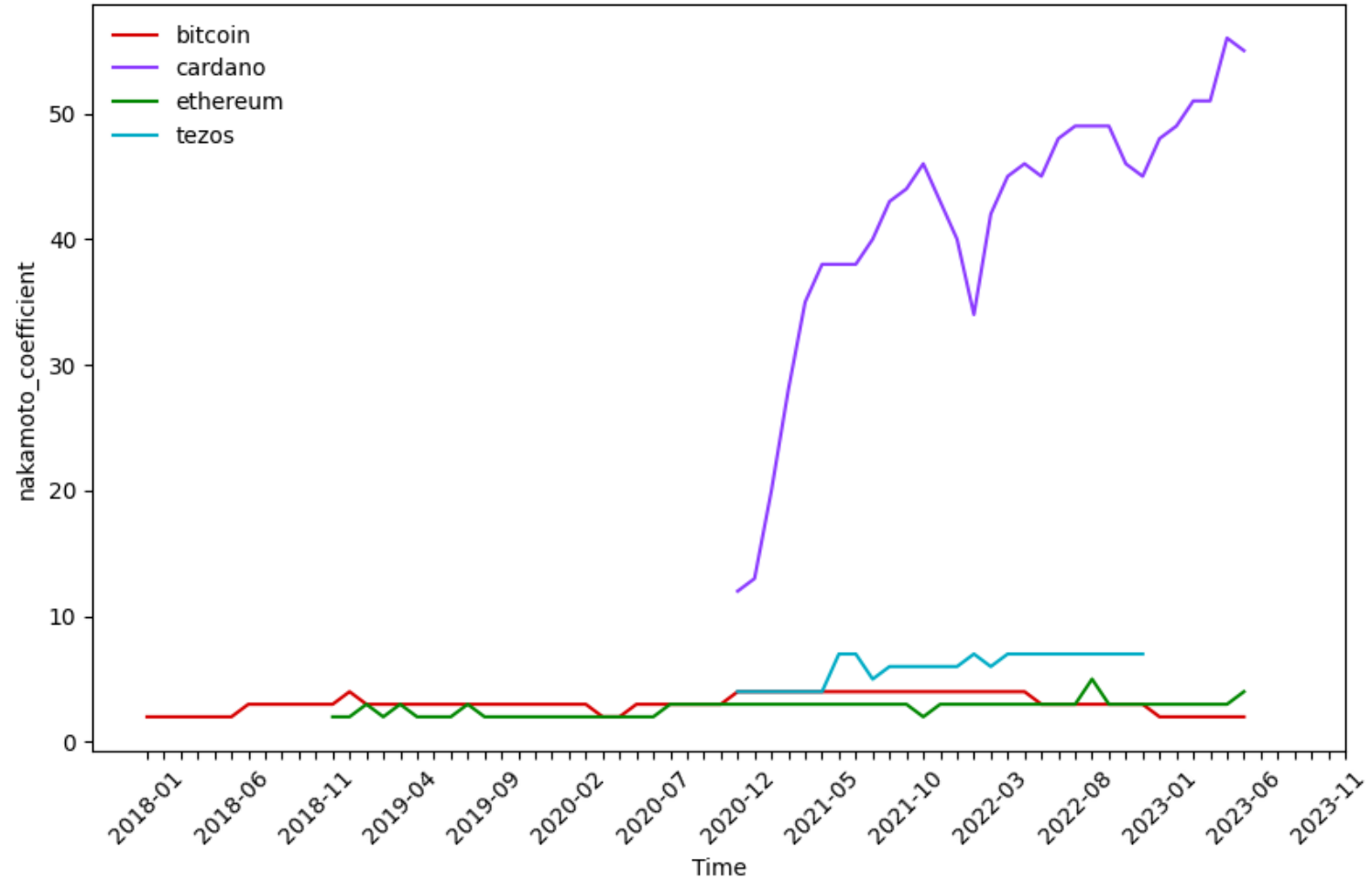
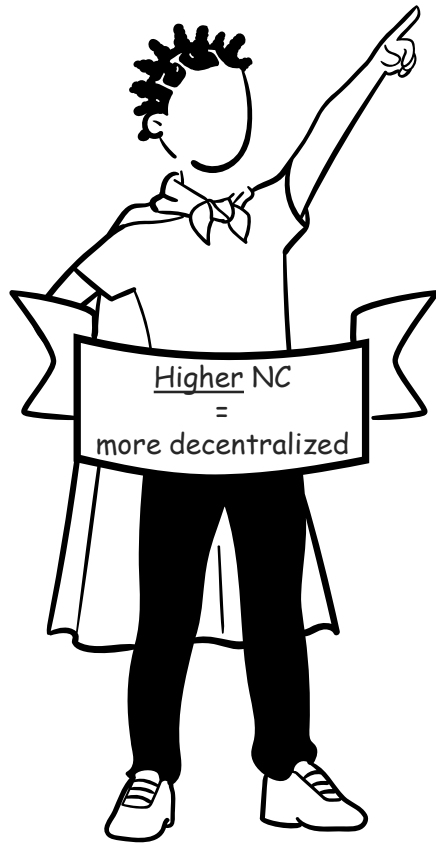
# Nakamoto coefficient

- Represents the **minimum number of entities** that collectively control a **majority of resources** ( $> 50\%$ )
- ..aka the number of parties that need to collude in order to launch a 51% attack
- The higher the Nakamoto coefficient, the higher the resilience to a majority attack



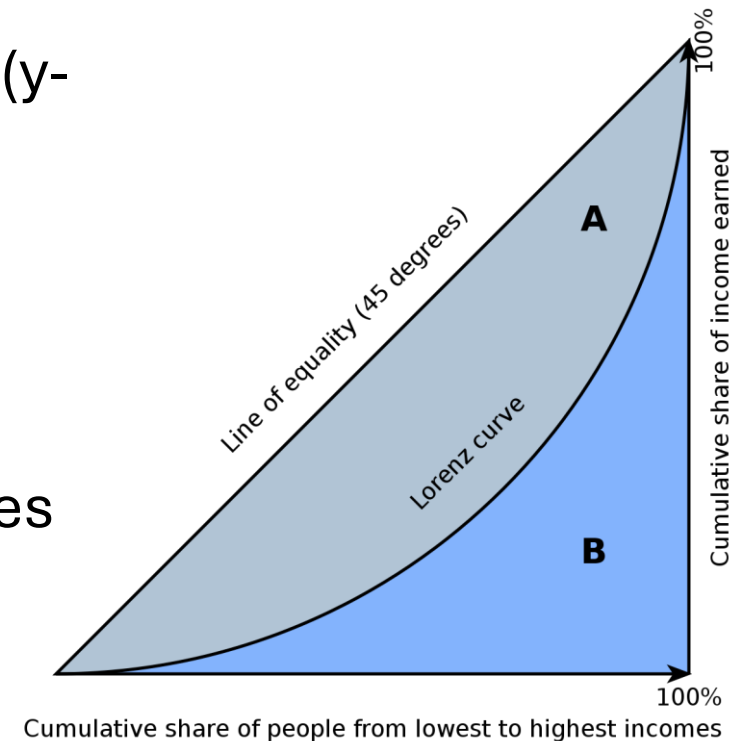


# Nakamoto coefficient

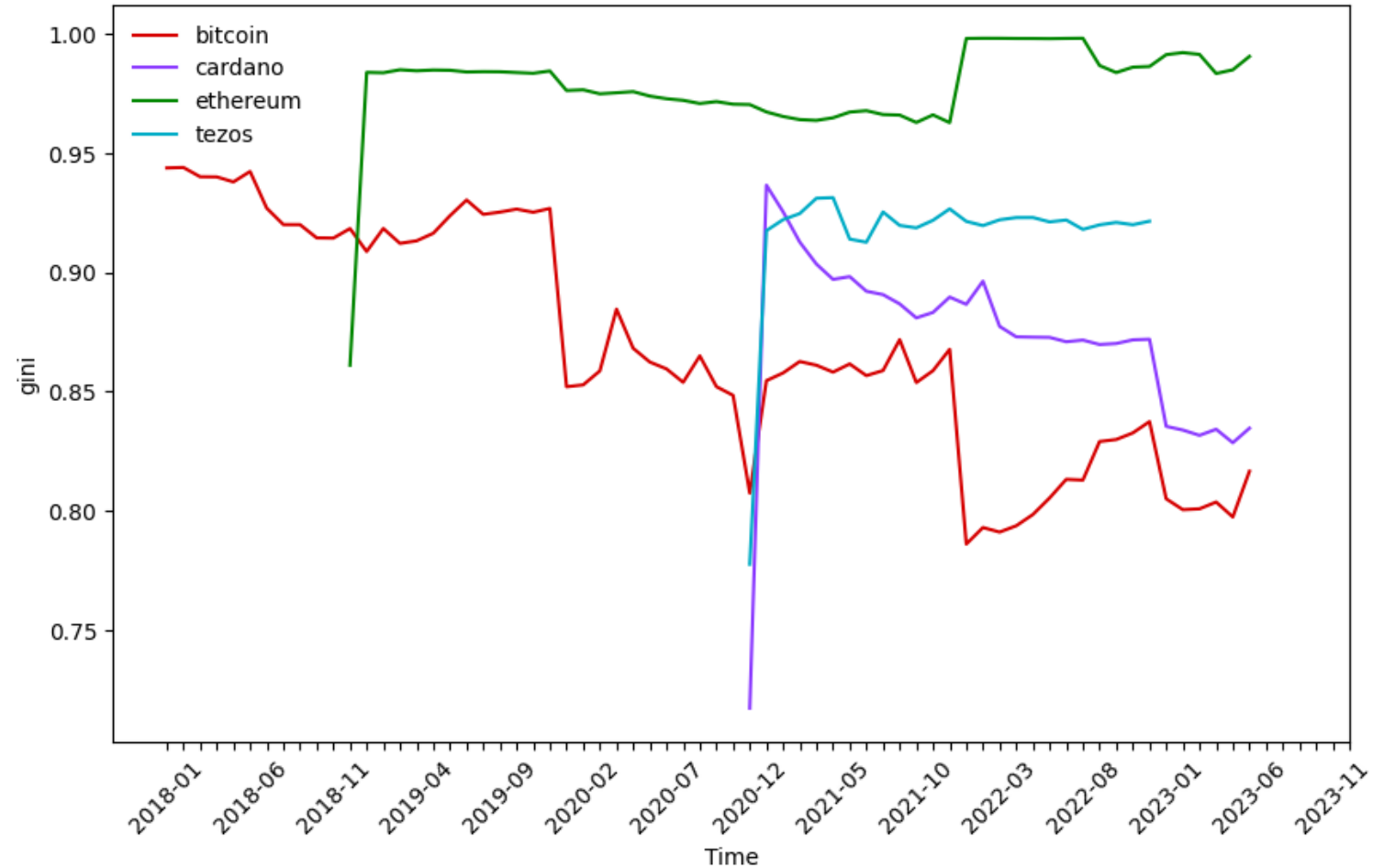


# Gini coefficient

- Lorenz curve of resources across entities
  - Points: the cumulative ownership of resources (y-axis) by a percentage of entities (in ascending order) (x-axis)
- Gini coefficient:  $A / A + B$
- Maximum equality  $\Rightarrow$  Gini = 0
  - Every entity holds the same amount of resources
- Maximum inequality  $\Rightarrow$  Gini = 1
  - One entity holds all resources



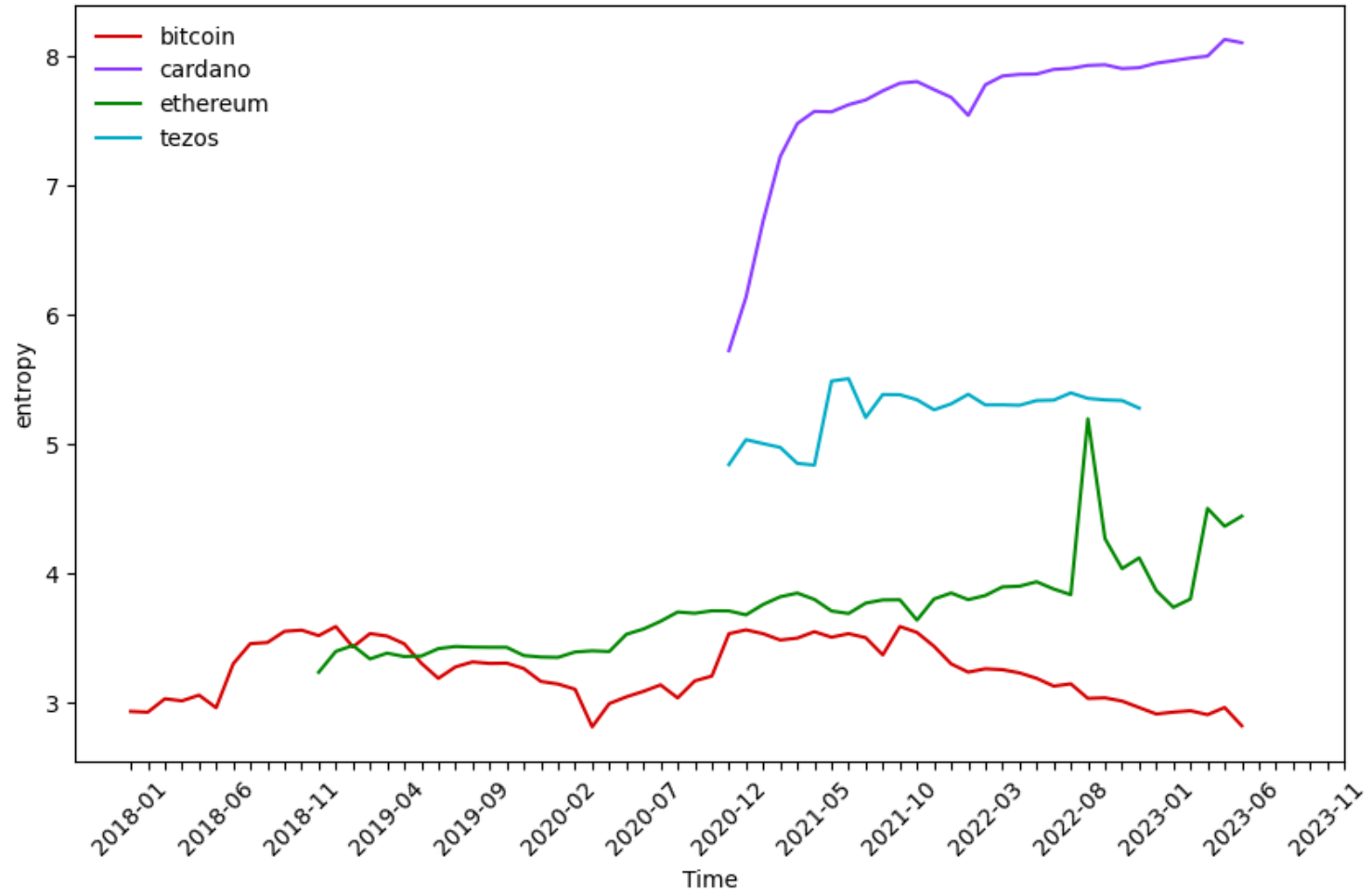
# Gini coefficient



# Shannon entropy

- The level (bits) of “information” in a distribution
  - $H(X) = - \sum ( p(x_i) * \log_2 p(x_i) )$  (X: random variable, p(x): probability of event X=x)
- In our case:
  - $\text{entropy}(S) = - \sum ( f(S_i) * \log_2 f(S_i) )$
  - $f(S_i)$ : the relative resources of entity  $S_i$  compared to all resources (as a percentage)
- Resources centralized around a few entities  $\Rightarrow$  Lower entropy
- Resources distributed among many entities  $\Rightarrow$  Higher entropy
  - Max entropy: when resources are evenly distributed among all entities

# Shannon entropy



# Herfindahl–Hirschman index (HHI)

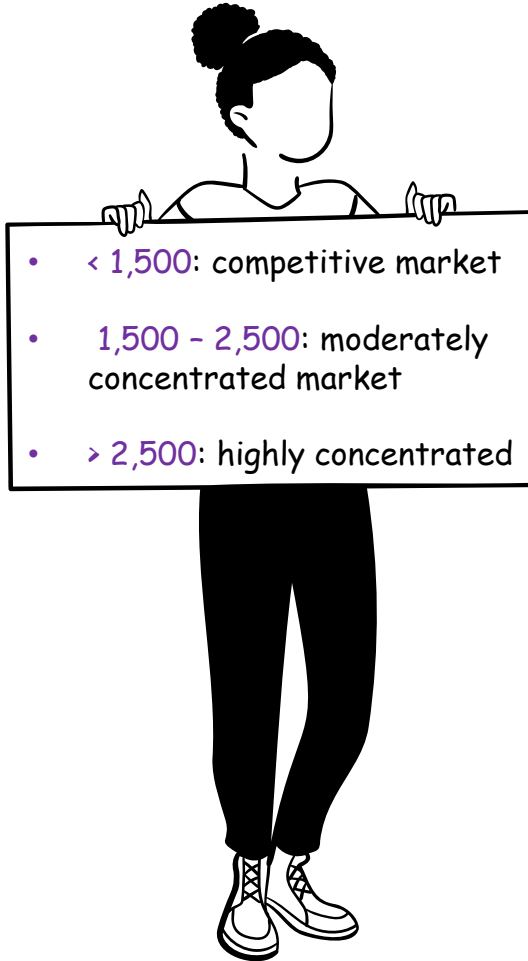
- Market concentration metric
- Can be calculated as follows:

$$HHI = \sum_{i=1}^n s_i^2$$

Where  $s_i$  is the market share of firm  $i$  (as a whole number, e.g. 20 for 20%)

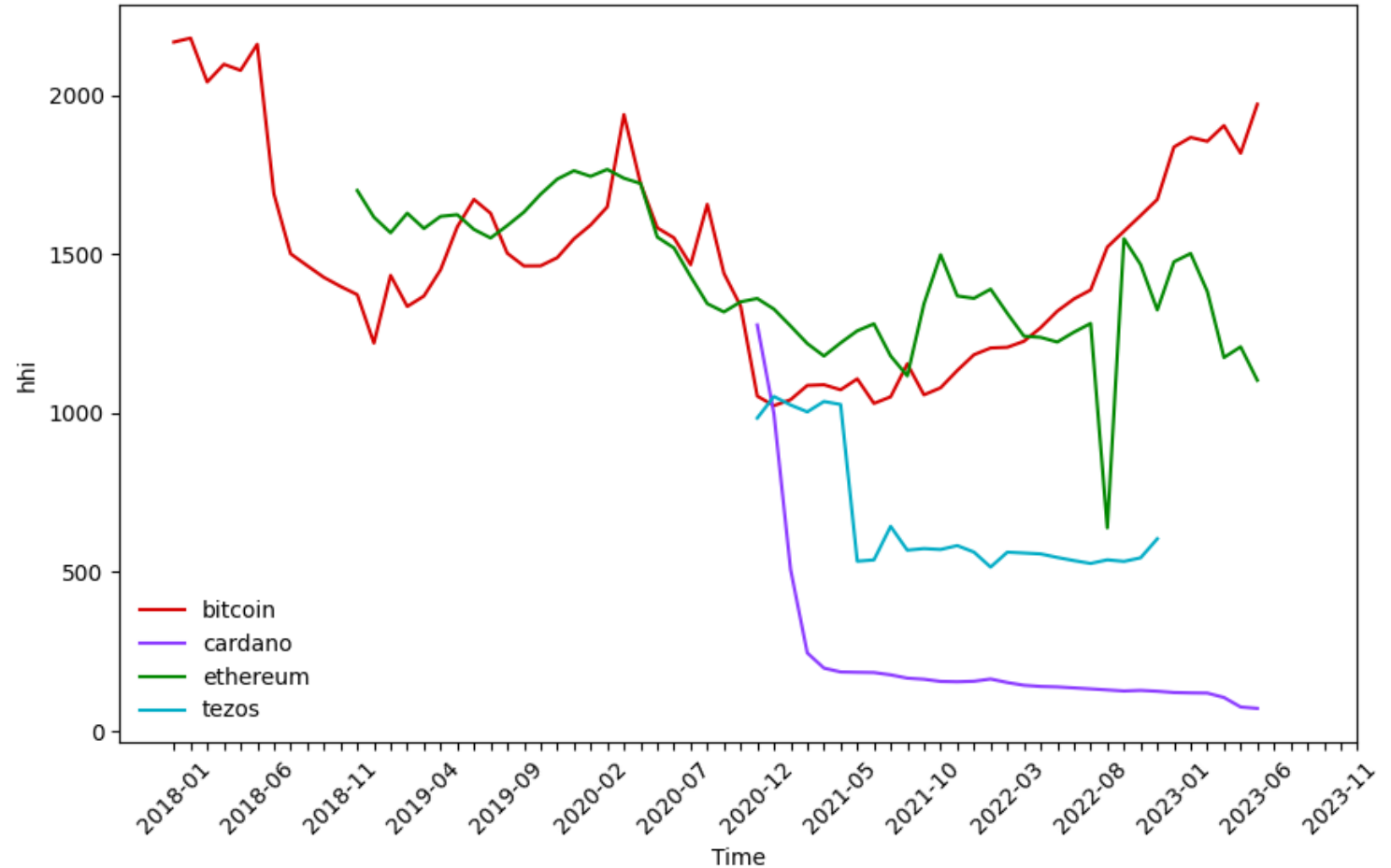
- U.S. Department of Justice guidelines:
  - $HHI < 1,500$ : competitive market
  - $1,500 \leq HHI \leq 2,500$ : moderately concentrated market
  - $HHI > 2,500$ : highly concentrated market
- Values chosen for traditional markets, may need different thresholds for blockchains

# Herfindahl–Hirschman index (HHI)



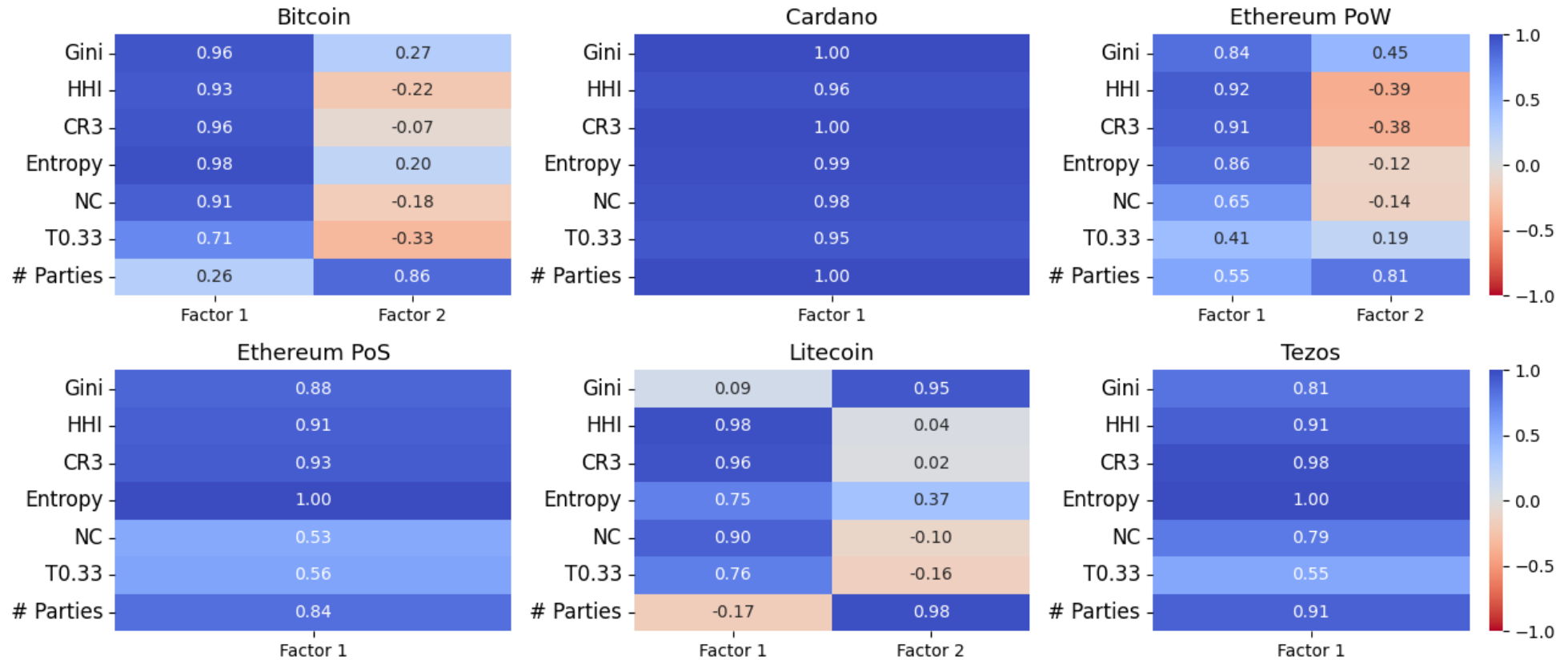
- < 1,500: competitive market
- 1,500 - 2,500: moderately concentrated market
- > 2,500: highly concentrated

U.S. Department of Justice



# Do all metrics capture the same signal?

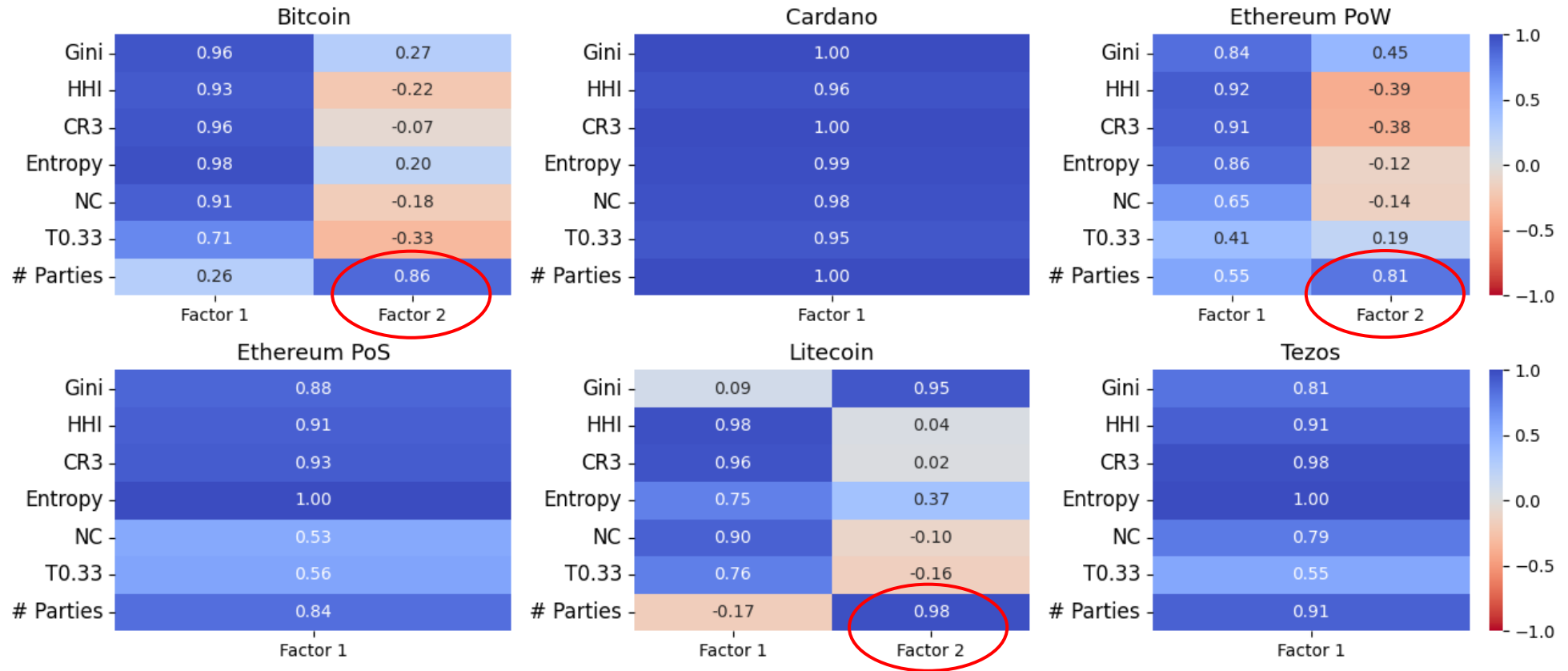
Consensus - Factor loadings





# Do all metrics capture the same signal?

Consensus - Factor loadings



# Open questions & future work

- How do different design choices or components impact decentralization?
  - Proof of Work vs Proof of Stake
  - Simple vs sophisticated reward schemes
  - Proposer-builder separation
- Can we merge all relevant metrics and layers into a single index that provides a holistic representation of a blockchain system's decentralization?



# Edinburgh Decentralization Index (EDI) Public dashboard

- Live public dashboard for multiple layers and systems:

<http://blockchainlab.inf.ed.ac.uk/edi-dashboard/>



Dashboard

alpha-release

Consensus

Tokenomics

Software



### Edinburgh Decentralisation Index

EDI™

The Edinburgh Decentralisation Index (EDI) studies blockchain decentralisation from first principles, archives relevant datasets, develops metrics, and offers a dashboard to track decentralisation trends over time and across systems.

[EDI Website.](#)

#### Tokenomics

This layer describes the decentralisation of token ownership over time.

#### Consensus

This layer describes the decentralisation of block production over time.

#### Software

#### Network (Coming Soon)



THE UNIVERSITY of EDINBURGH  
**informatics**

# Thank you!

# Questions?

[christina.ovezik@ed.ac.uk](mailto:christina.ovezik@ed.ac.uk)

